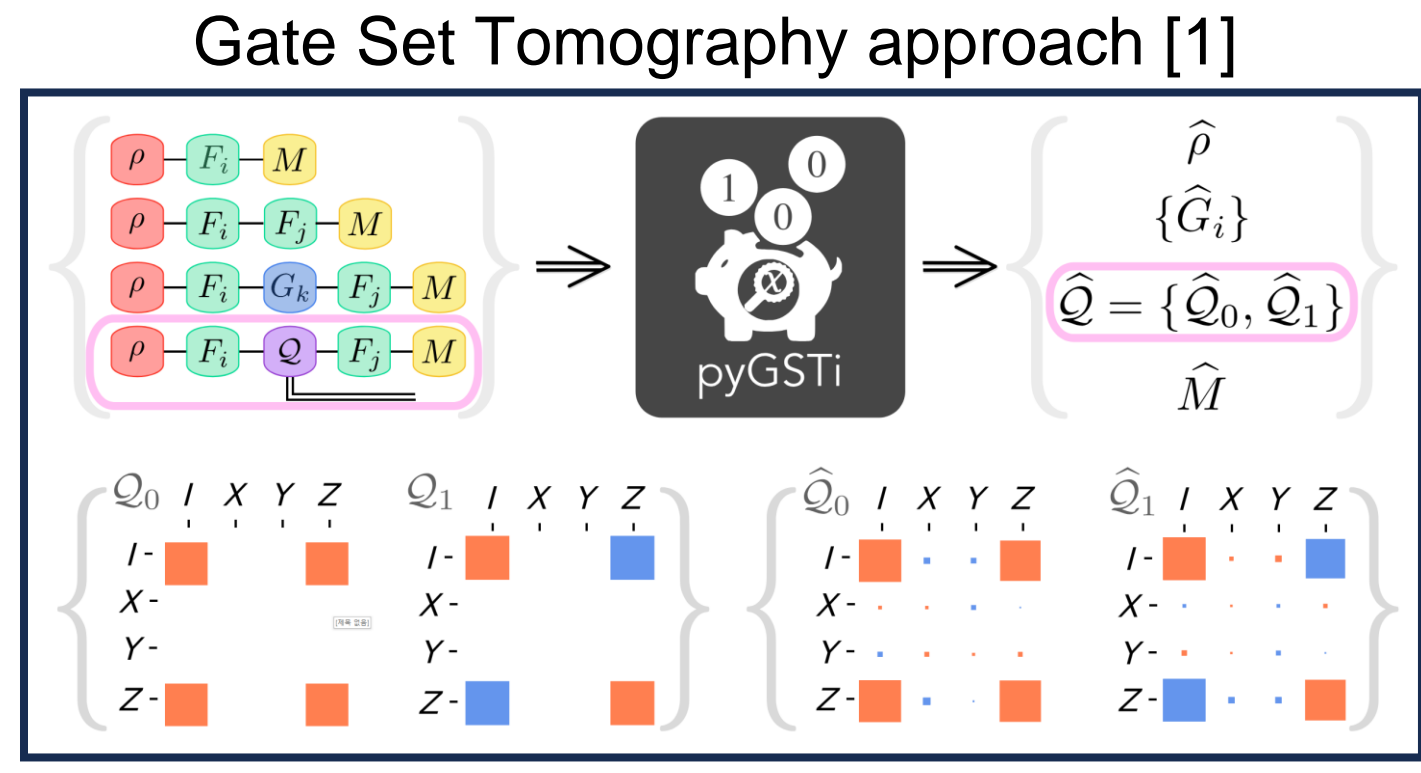
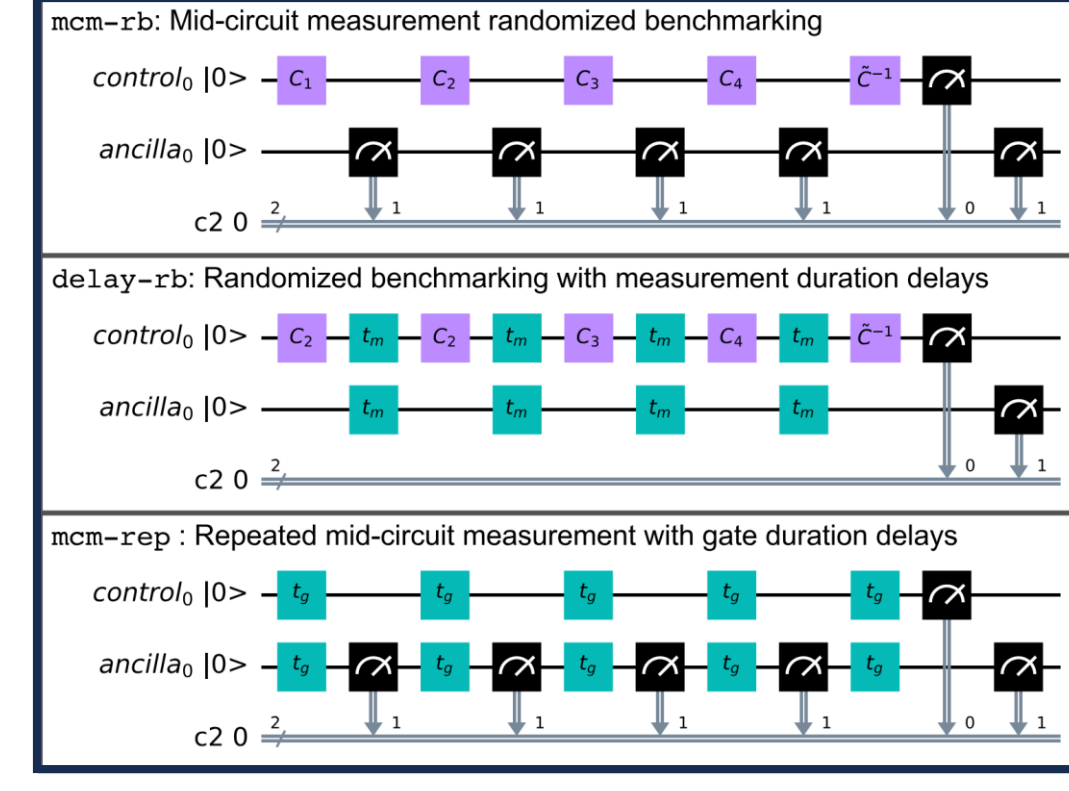


## Motivation

- Mid-circuit measurements (MCMs) are core building blocks for fault-tolerant quantum computing.



Randomized benchmarking approach [3]



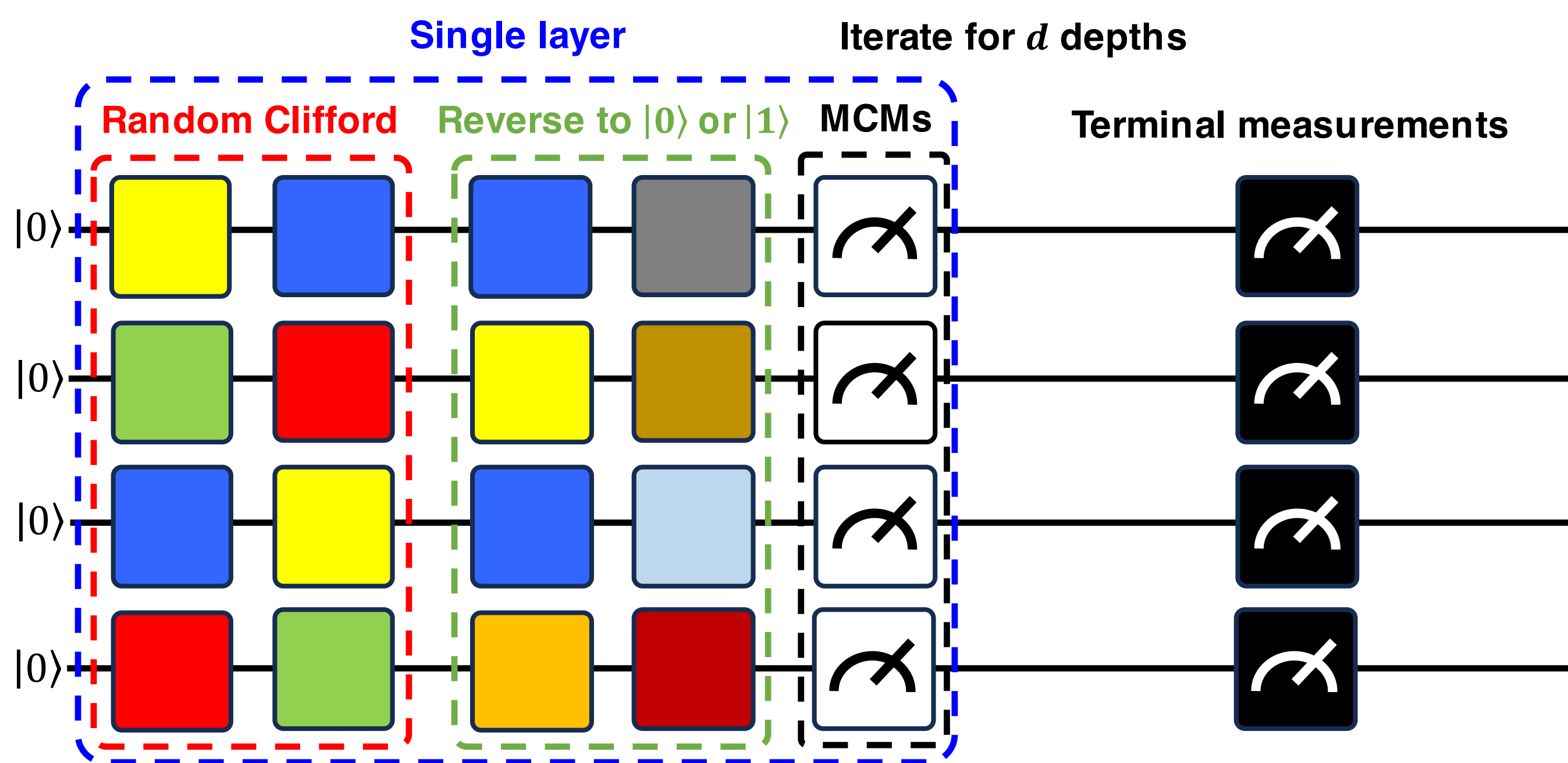
- Randomized benchmarking has the advantage of efficiency and scalable average fidelity measurements, in contrast to tomography based methods which provide detailed but non-scalable characterizations. [1-3].

- An efficient and scalable benchmarking protocol capable of characterizing and measuring the error rates of MCMs will serve as a good testbed for calibration and optimization of MCMs.

## Randomized benchmarking with interleaved MCMs layers

### Scheme 1

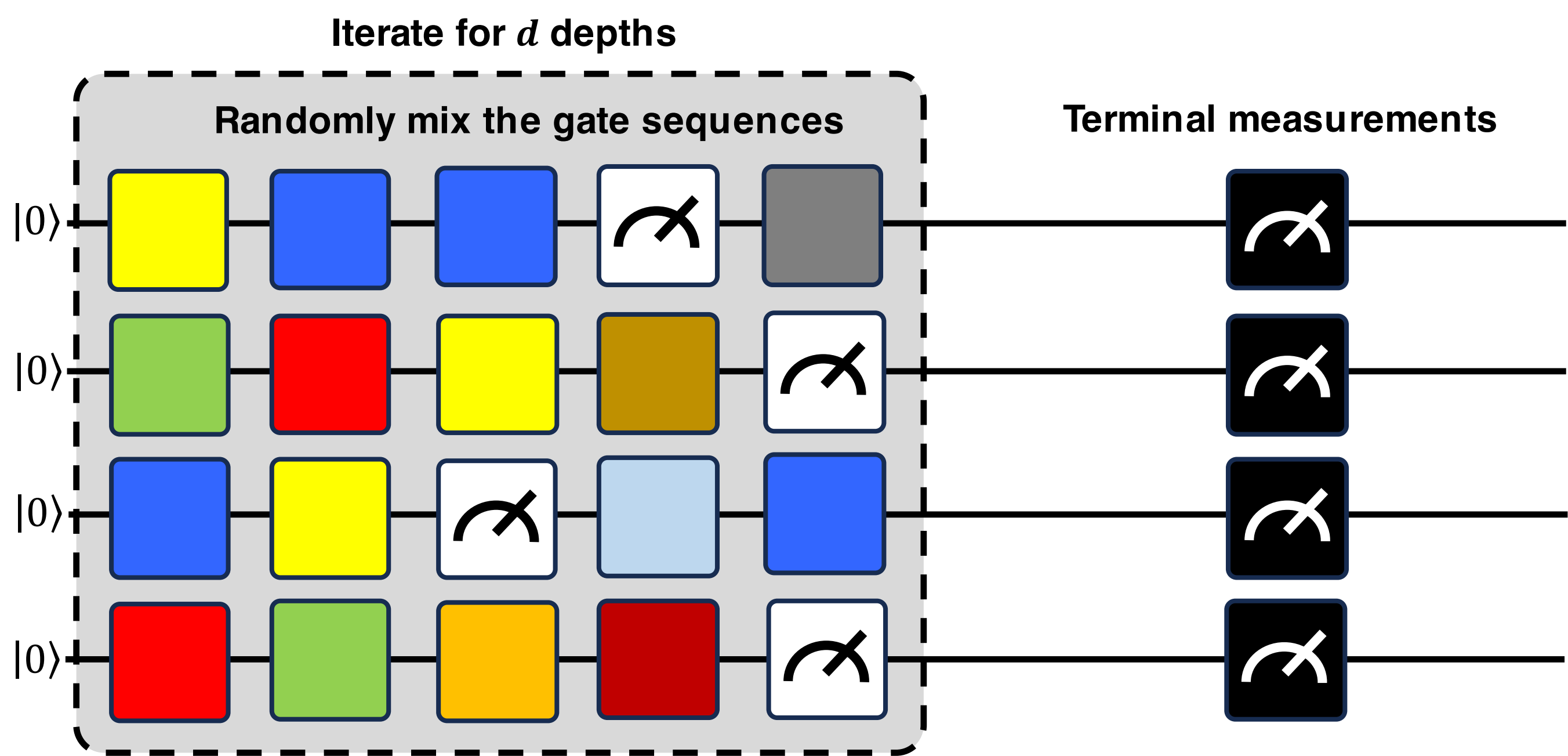
Effectively Measurement-induced control error free



- MCMs and single qubit gates are not performed at the same time which effectively prevents measurement-induced control errors from qubits.

### Scheme 2

Measurement-induced control error added



- Mixing the gate sequences enables single qubit gates and MCMs to be overlapped so that measurement-induced control errors can be added.  
- By adjusting the rate of qubit reversal to 0 or 1, state-dependent errors such as the residual ZZ interaction can be tuned.  
- MCM errors are extracted using interleaved randomized benchmarking.  
- Controlling the overlap between MCMs and single qubit gates is crucial.

## Error signatures of MCMs [3]

### Measurement induced control error

#### Stark shift error

$$\hat{U}_{\text{Stark}} = e^{-i\phi\hat{\sigma}_z}$$

$\chi$ : dispersive shift.  
 $\bar{n}$ : mean photon number in readout resonator.  
 $\phi = 2\chi\bar{n}T$   
 $T$ : measurement duration.

#### Cross-measurement error

$$\hat{K}_0 = \sqrt{p_m}|0\rangle\langle 0|$$

$$\hat{K}_1 = \sqrt{p_m}|1\rangle\langle 1|$$

$$\hat{K}_2 = \sqrt{1-p_m}\hat{I}$$

$p_m$ : cross-measurement probability

### Local measurement error

#### Non-QND error

$$\varepsilon_{\text{dep}}(\rho) = (1-\eta)\rho + \eta\frac{\hat{I}}{2}$$

$\eta$ : depolarization probability

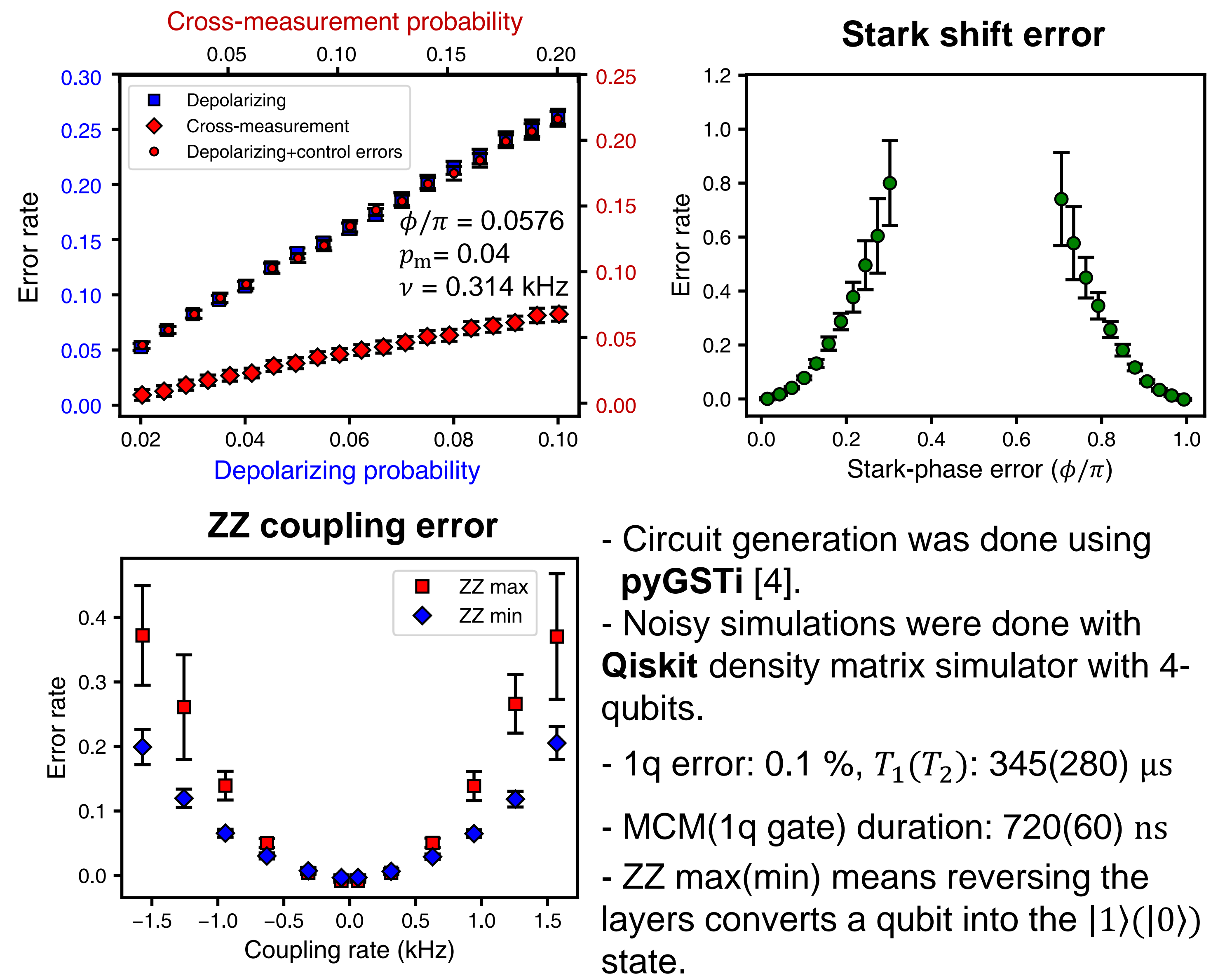
#### Residual ZZ interaction

$$\hat{U}_{\text{ZZ}} = e^{-i\hat{H}_{\text{ZZ}}T}$$

$$\hat{H}_{\text{ZZ}} = v|e\rangle\langle e|_{\text{measured}} \otimes \hat{\sigma}_z^{\text{neighbor}}$$

$v$ : coupling rate

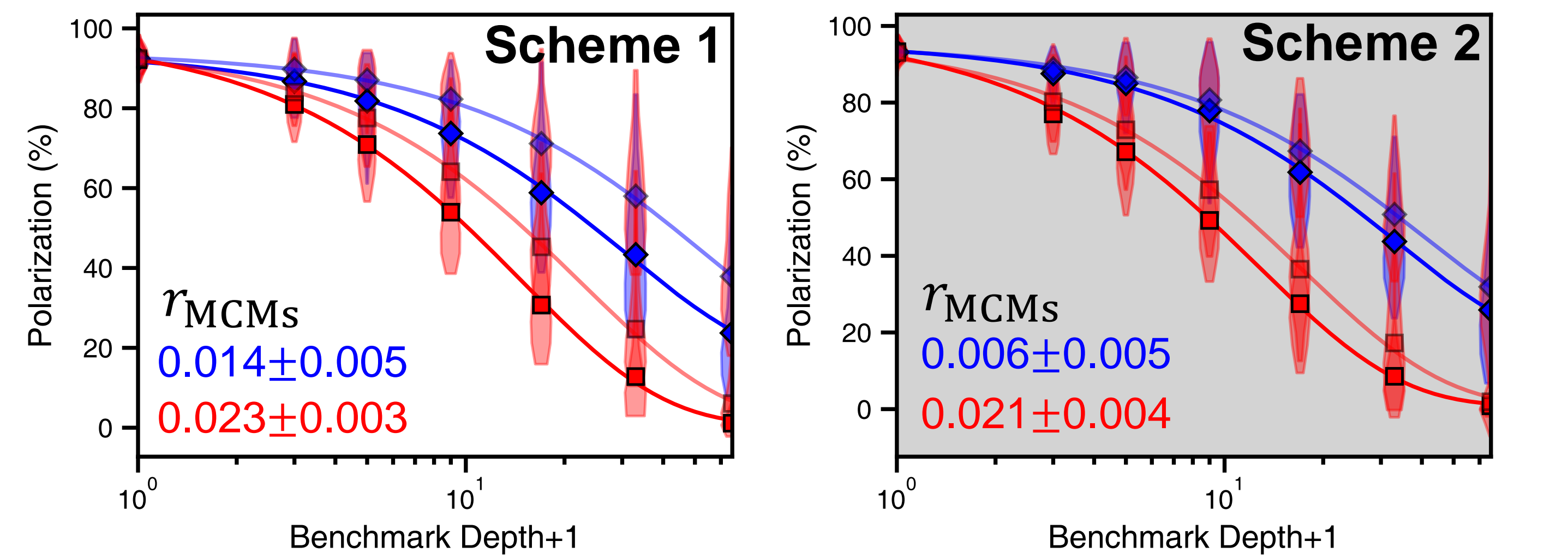
## Noisy simulation results



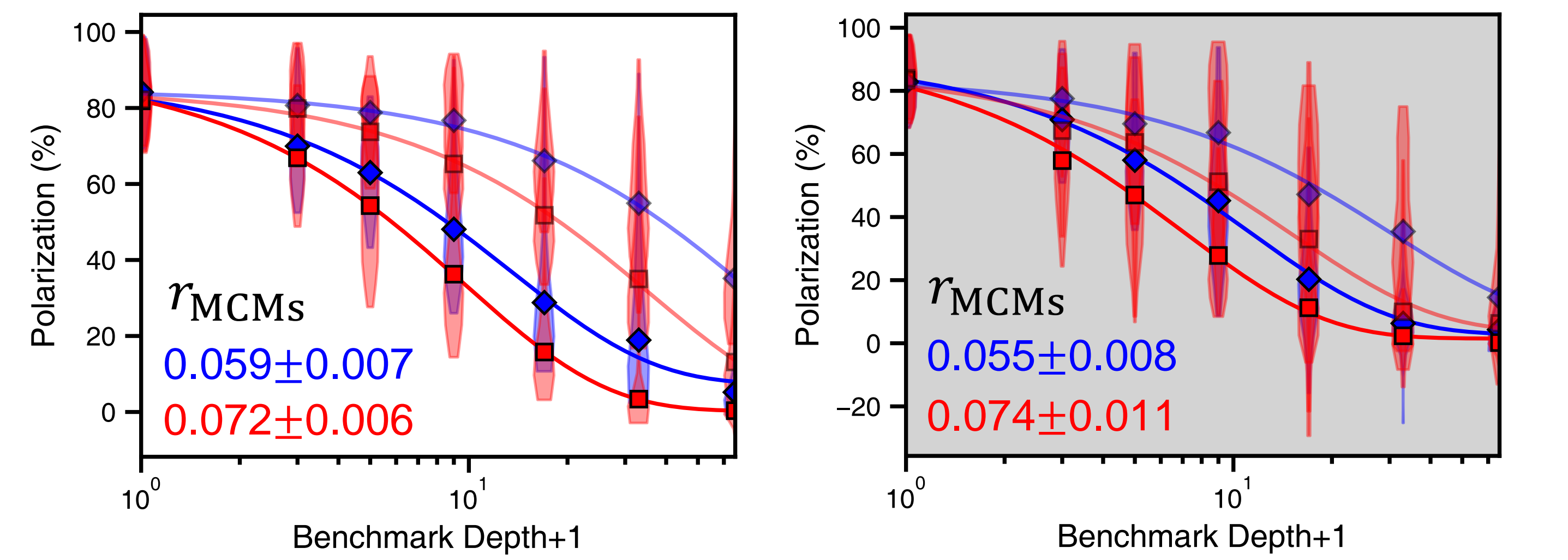
## IBM backend results

On 127-qubits systems, 4-qubits are used.  
Number of shots = 10000

1. **ibm\_brisbane**: qubits = [63, 64, 65, 66]



2. **ibm\_osaka**: qubits = [63, 64, 65, 66]



## Calibration data

Brisbane (Osaka)	Readout assignment error	Prob. meas0 prep1
q[63]	0.0060 (0.0097)	0.0048 (0.0106)
q[64]	0.0063 (0.0086)	0.0080 (0.0102)
q[65]	0.0166 (0.0113)	0.0200 (0.0132)
q[66]	0.0698 (0.00863)	0.0494 (0.0084)

MCMs parameters  
 MCMs duration: 720 (720) ns  
 Depopulating time after MCMs: 1640 (340) ns

## Conclusion

- Randomized benchmarking based schemes ensure scalability and efficient measurement of MCM errors.  
- Adjusting the gate and MCM timing enables characterization of the error signatures of MCMs.  
- Demonstration of benchmarking protocol both on a noise simulator and superconducting qubit systems-ibm\_brisbane and ibm\_osaka.

## References

- [1] K. Rudinger et al., Phys. Rev. Appl. 17, 014014 (2022).
- [2] J. P. Gaebler et al., Phys. Rev. A 104, 062440 (2021).
- [3] L. C. G. Govia et al., New Journal of Physics 25, 123016 (2023).
- [4] Nielsen, Erik, et al., Quantum science and Technology 5.4, 044002 (2020).

## Acknowledgement

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